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SRI Framework
Theory

Rp001 2017272 (Sound Risk Indicator)

25 March 2020

PROJECT: SOUND RISK INDICATOR FRAMEWORK - THEORY

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REPORT NO.: Rp005 2017272 (Sound Risk Indicator – Theory)

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Document Control

Status:	Rev:	Comments	Date:	Author:	Reviewer:
Final	2.0		25 March 2020	Rasmus Sloth Pedersen <i>Rasmus Sloth Pedersen</i>	Jürgen Weissenberger <i>J. Weissenberger</i>

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31 **1.0 MOTIVATION**

32 Assessing the impact of underwater noise is a complicated task. There are multiple reasons for
 33 this, many of whom relate to the complexity of the marine habitats as well as the fauna within it.
 34 For an accurate assessment it is necessary to consider all these factors. We argue that this
 35 complexity can cause some confusion along with large variability in the quality of assessment,
 36 leading to potential distrust, and therefore disregard for underwater noise assessments. Given the
 37 importance of our marine resources such a scenario is highly unfavourable.

38 As noise propagation modelling can be a cumbersome and slow procedure, we propose the use of
 39 a **Sound Risk Indicator** (SRI) value being assigned to a noisy activity early on in the design phase.
 40 This value can be used as a guide to rapidly assess what effect changes to the activity have on the
 41 environmental acoustic impact of the activity. With changes in the activity the SRI can quickly be
 42 updated and will either increase (more noisy) or decrease (less noisy) in response to changes in
 43 activity methods. In this way the framework and associated software tool can help in planning
 44 activities while continually keeping an eye on the environmental acoustical impact changes.

45 This report is one part of a two-part framework:

46 **1. Theory (This document)**

47 In this document the theoretical background for a method to index noisy marine activities is
 48 described. The purpose of this document is to guide the reader through the theoretical
 49 considerations forming the background of the calculation of a Sound Risk Indicator (SRI).

50 **2. Suggestion for application and examples (SRI Methods)**

51 The methods described in this document will be applied with suggested marine animal acoustic
 52 weightings as well as examples of practical usage. The “SRI-Tool” (software package) will also be
 53 presented here.

54

55 *The reader of this document is asked to remember that the sole purpose of this document is to*
 56 *describe the methods for calculating a Sound Risk Indicator from a rather limited information*
 57 *base, and not to discuss propagation losses nor the ecosystem impacts of anthropogenic noise.*

58

1.2 ABBREVIATIONS

SRI	Sound Risk Indicator
dB	decibell, 0.1 x Bell: logarithmic unit used for sound pressure ratios
SEL	Sound Exposure Level
z-p	“zero-to-peak”
p-p	“peak-to-peak”
RMS	Root Mean Square
TL	Transmission Loss, in dB unless otherwise stated
ICC	Irwin Carr Consulting
NOAA	National Oceanic and Atmospheric Administration (of USA)
TTS	Temporary Threshold Shift
PTS	Permanent Threshold Shift
Timeseries, TS	A series of pressure values sampled with a constant time interval
dBSea	Underwater noise propagation modelling and visualisation software
SH2019	According to (Southall, et al., 2019)

59

60 2.0 INTRODUCTION

61 In this document we propose that with a highly simplified approach one can index noisy activities in
 62 such a way that a reduction of a calculated index value (Sound Risk Indicator, **SRI**) will result in a
 63 real-world reduction of environmental acoustic impact. We also describe the methods and
 64 considerations behind this proposal. While we repeatably use theory from the acoustic propagation
 65 modelling literature, this is *not an exercise in acoustic modelling*. The methods described here will
 66 lead to an index value (SRI), based on a relatively small amount of initial information about the
 67 environment and the sound source(s) involved.

68 This approach assumes a scenario where the user has limited or incomplete information about the
 69 activity, the surroundings and the presence of acoustically sensitive species.

70 In general, the SRI rests on a principle of quantifying the area affected by a noisy activity in a
 71 fictitious environment by using simple logarithmic spreading models and absorption. By
 72 introducing spectral information of the source, the receiver and a threshold, a corresponding range
 73 to that threshold can be calculated.

74 The area given by this range is used to calculate the SRI.

75 ***The use of transmission models is not an attempt to calculate real-world propagation, but solely to***
 76 ***have a standardised way of generating an index number from initial values. The logarithmic***
 77 ***propagation models were chosen as they ensure that SRI scales well with changes in source level***
 78 ***and receiver sensitivity.***

79 This document focuses on the considerations and calculation methods behind the tool.

80 2.1 ADDITIONAL USES

81 A separate use for the tool, besides the primary goal of assisting comparisons, is that we here use
 82 a propagation model that aims to find the smallest realistic transmission loss. This has the effect
 83 of providing some real-world reference to the model, and further makes real-world impacts larger
 84 than the predicted very unlikely. This is not the main purpose of the tool, but rather a consequence
 85 of the applied methods.

86 2.2 UNITS

87 Throughout this document we will strive to be consistent and strict in the use of terminology
 88 relating to units and here bring an overview of the definitions used:

89 **Table 1. Units used throughout the report. Please see ISO 18405-2017 for more details.**

Unit	Definition	Comments
dB_{RMS} ISO 18405- 2017: 3.2.1.1	$dB_{RMS} = 10 \cdot \text{Log}_{10} \left(\frac{1}{t_2 - t_1} \cdot \int_{t_1}^{t_2} p(t)^2 dt \right)$	Functionally equivalent to depreciated $20 \cdot \text{Log}_{10} \left(\frac{RMS}{1 \cdot 10^{-6} Pa} \right)$
dB_{z-p} ISO 18405- 2017: 3.2.2.1	$dB_{z-p} = 20 \cdot \text{Log}_{10} \left(\frac{Pa_{max}}{1 \cdot 10^{-6} Pa} \right)$	This assumes that Pa_{max} is equal or greater than $\sqrt{Pa_{min}^2}$
dB_{p-p} ISO 18405- 2017: 3.1.2.8	$dB_{p-p} = 20 \cdot \text{Log}_{10} \left(\frac{Pa_{max} - Pa_{min}}{1 \cdot 10^{-6} Pa} \right)$	Often ¹ equivalent to $dB_{z-p} + 6.02 \text{ dB}$
dB_{SEL} ISO 18405- 2017: 3.2.1.5	$dB_{SEL} = 10 \cdot \text{Log}_{10} \left(\frac{\int_{t_1}^{t_2} p(t)^2 dt}{1 \cdot 10^{-12} Pa} \right)$	For continuous sound this is equivalent to $dB_{RMS} + 10 \cdot \text{Log}_{10}(t_2 - t_1)$

90 Additional to the above units we might indicate a time associated with the unit. E.g. “ $dB_{SEL-24h}$ ” is
 91 taken to mean the dB_{SEL} value over a 24-hour interval, “ $dB_{SEL-impulse}$ ” is the dB_{SEL} value of a single
 92 impulse and “ $dB_{RMS-1000}$ ” is the dB_{RMS} value with an averaging window of 1000 milliseconds.

¹ If pulse is below ambient pressure and compression and rarefaction phases are of equal size.

93 **3.0 THE SOUND RISK INDICATOR**

94 The SRI value comes from the simplified range calculation to a frequency weighted limit. The SRI is
95 thus equal to the radius in kilometers of a circle of the same area as the area where the limit is
96 exceeded.

97 For single point sources:

98
$$SRI = R_{Limit} \tag{1}$$

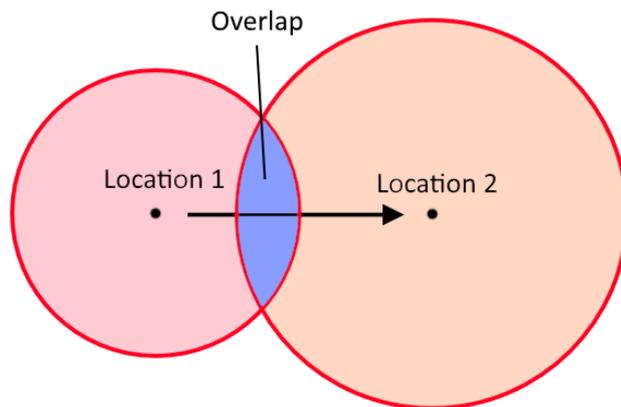
99 With R_{Limit} being the range to the limit. For multiple source or moving sources the SRI becomes
100 slightly more complicated as there can be an overlap in areas from one source position and the
101 next.

102 Here it is important to differentiate between two different operating modes of the SRI-tool:

103 **1. Geometry mode:**

104 No propagation calculation takes place. The tool uses source position(s) and R_{Limit} to
105 create a series of circles. The total area of these circles is then calculated, taking the
106 possible overlap of one or more circles into account, so that overlapping areas are not
107 counted more than once. No area outside the impact circle(s) is included in the basis for
108 the SRI (Figure 1). Also, this mode ignores land.
109

110 **Figure 1. Overlapping areas from two source positions.**



111
112

113
$$SRI_{Geometry-mode} = \sqrt{\frac{\sum_{i=1}^{i=n} A_{Location\ i} - A_{overlap}}{\pi}} \tag{2}$$

114 With " $A_{Location\ i}$ " being Area related to source location " i " and " $A_{overlap}$ " the additional area
115 from overlap. For more sources more overlaps become possible, and with e.g. four source
116 positions, areas can overlap with areas from three other source positions and two other
117 overlaps.

118 In all cases it's the combined area that forms the base for the "Geometrical mode-SRI".

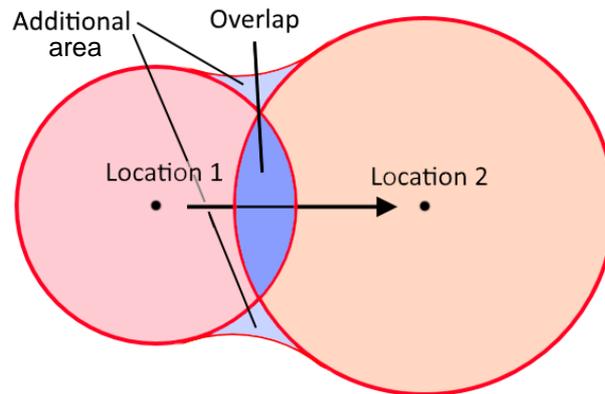
119 **2. Transmission Loss mode (TL-mode):**

120 The tool uses the transmission loss model described in section 4.0, p. 8 to calculate
121 levels throughout the scenario. This means that areas that fall outside the R_{Limit} for one
122 source position, if it was alone, can be brought over the limit by contributions from other
123 sources (Figure 2, p. 8). This effect is especially relevant for cumulative sound exposure
124 and multiple or moving sources.

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Figure 2. When calculating SRI for multiple source locations in TL mode, cumulative limit types mean that additional area will be brought over the limit. Here labelled “Additional area”.



128

129

$$SRI_{TL-mode} = \sqrt{\frac{\sum_{i=1}^{i=n} A_{Location\ i} - A_{duplicate\ overlap} + A_{additional}}{\pi}} \quad (3)$$

130

131 The two operating modes will give very similar result for single sources², while some divergence is
132 expected for moving sources.

133 The final SRI is thus the radius of a circle with an area equal to the impact area, e.g. in a simple
134 case (Figure 2) the radius in km of a circle with the same area as the combined area of both circles
135 and the additional area.

136 3.1.2 SRI from different types of limits

137 In the literature for marine animal impact e.g. (Carlson, Hastings, & Popper, 2007; NOAA, 2018;
138 Popper, et al., 2014) the limits are often in two categories:

- 139 1. Cumulative impact, continuous or impulsive noises.
140 Energy exposure is accumulated over time, with repeated exposures adding up to the
141 total exposure level. Limits associated with this form of impact is given as dB_{SEL}, and often
142 over a 24-hour time period.
143
- 144 2. Instantaneous impact of impulsive noises.
145 The limit is given as dB_{Z-p} or dB_{p-p}. When assessing impact associated with this type of
146 limit repeated exposures are not accumulated, and only a single impulse is assessed.

147 In the tool, these two noise- and limit-types are treated differently for multiple source positions as
148 one type is for accumulated energy and the other is not. Thus multiple exposures with dB_{Z-p} or dB_{p-p}
149 limits yield the same SRI as for a single exposure with those limit types (as long as the source is
150 stationary). For limit type dB_{SEL}, multiple occurrences accumulate, and thus inflate the SRI.

151 4.0 TRANSMISSION LOSS CALCULATION – BASE MODEL

152 The area/range for the SRI is determined using a simplified model based on spherical/cylindrical &
153 absorption transmission loss with some modifications to ensure robustness across more scenario
154 types. Below is a short overview of the background of the transmission loss model that is mostly
155 based on work by (Duncan & Parsons, 2011), but with further additions to make their model more
156 general.

157 (For details please see Duncan & Parsons (2011)³ - they detail the adaption of the spherical/
158 cylindrical model described in by Urlick (1983) but adopted to estimate minimal transmission loss).

² Provided the results grid resolution is sufficiently high (the tool will warn the user)

³ We recommend that you read this paper, available from:
https://www.acoustics.asn.au/conference_proceedings/AAS2011/papers/p87.pdf

159 Results from the transmission loss calculation are stored in a 3D grid of receivers that are later
 160 used when determining ranges to limits according to receiver sensitivity (section 5.3, p. 15).

161 Note that the model in Duncan & Parsons (2011) assumes flat (constant depth) bathymetry, while
 162 the SRI tool will use the depth at the source as a basis for calculation.

163 The choice of this simplistic approach was based on a desire to evaluate *minimal* transmission
 164 loss rather than *probable* transmission loss, while keeping it simple enough for fast calculations
 165 and consistent application across a wide range of scenarios.

166 A simple cylindrical spreading approach (TL = 10Log₁₀(range)) will greatly underestimate
 167 transmission losses, especially for deeper water, and therefore not attractive in this framework.

168 A simple spherical model (TL = 20Log₁₀(range)) was discarded for the reason that it tends to
 169 overestimate transmission losses (ignoring reflections and refraction).

170 The mixed model from Duncan & Parsons (2011) accounts for depth and incorporates a statistical
 171 measure to limit risk of overestimating transmission loss.

172 Transmission loss equation from Duncan & Parsons 2011:

$$173 \quad TL = 10 \cdot \text{Log}_{10}(r) + 10 \cdot \text{Log}_{10}\left(\frac{D}{2}\right) - B + \alpha \quad (4)$$

174 “TL” is transmission loss in dB, “r” is horizontal range from source in meters, “D” is depth at source
 175 location⁴ in meters and “B” is a correction in dB used to adjust the probability of overestimating
 176 the transmission loss⁵. This correction is applied to counter the fact that levels are not evenly
 177 distributed in the water volume.

178 In calculating transmission loss for a particular range, some parts of the sound field will experience
 179 higher levels than the mean, and other parts of the sound field will experience lower levels.

180 It’s assumed, due to the range of environmental factors that affect the exact sound field that the
 181 central limit theorem will apply, and the intensity will conform to an exponential probability
 182 distribution. Under this assumption, pressures will conform to a “Rayleigh distribution⁶”, the base
 183 of this assumption is further explained in Duncan & Parsons (2011).

184 Solving for “r” in Eq. 4 gives the range at which a given TL is expected. By choosing this TL so that
 185 it is equal to the source level minus the limit we are interested in, a range to the limit can be found:

$$186 \quad r = 10^{\left(\frac{TL+B-10 \cdot \text{Log}_{10}\left(\frac{D}{2}\right)}{10}\right)} \quad (5)$$

187 To define “B” we return to Duncan & Parsons (2011), p. 3 where they cite the results of another
 188 study (Shepherd & Milnarich, 1973) to define a probability function for a given level in the sound
 189 field exceeding the calculated mean level:

190 The probability that a level “l” at any point exceeds the mean level by “y” dB is then given by:

$$191 \quad P_{l>y} = e^{(-e^{0.23026 \cdot y})} \quad (6)$$

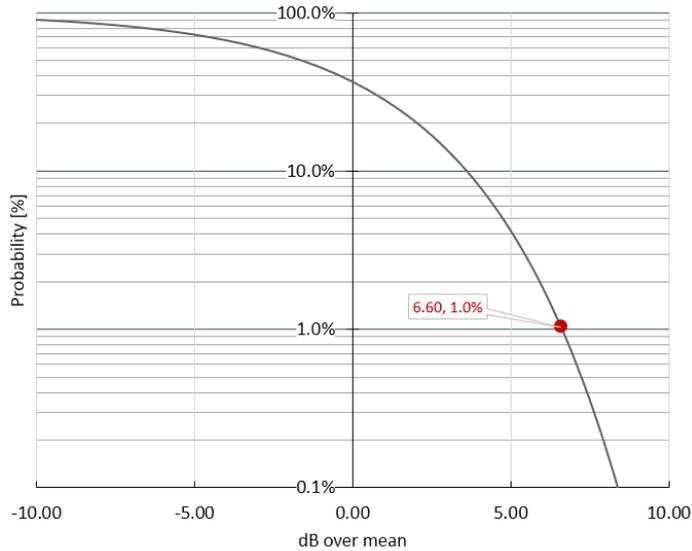
⁴ This framework uses “D” (depth) as a constant (deviating from (Duncan & Parsons, 2011)), and therefore assumes flat seabed/uniform depth.

⁵ Overestimating transmission loss leads to a lower SRI

⁶ A continuous probability density function characteristic of scenarios with multiple uncorrelated & normally distributed variables.

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Figure 3. Plot of Eq. 6. Probability that a level is 'y' dB above the predicted mean level. Example call-out at suggested probability of exceedance of 1% (6.6 dB).



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Solving Equation 6 for “y”:

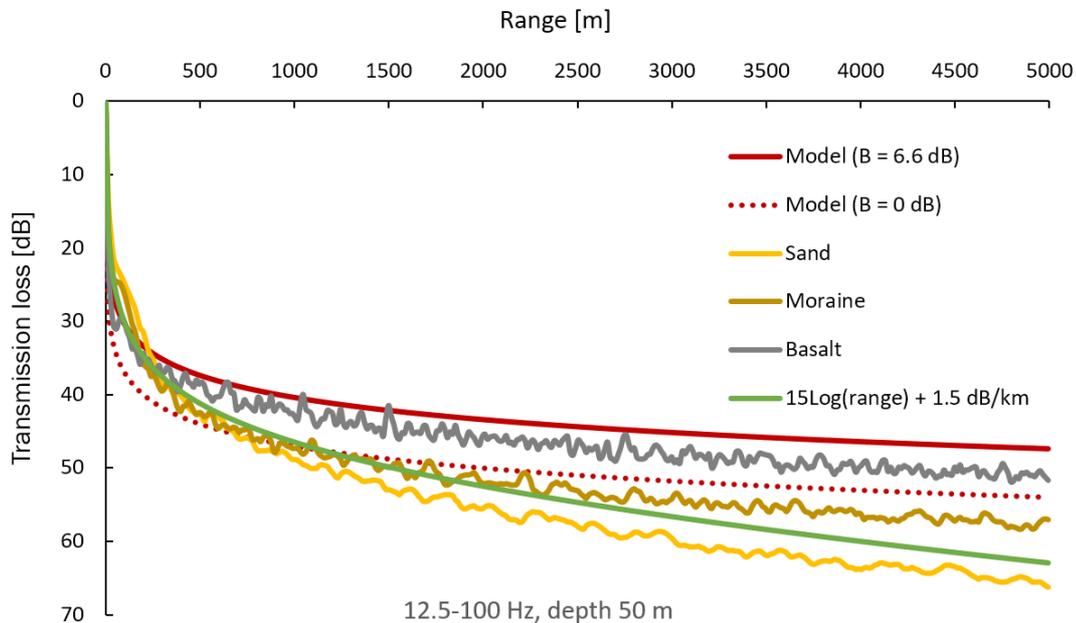
$$y = \frac{\ln(-\ln(P_{I>y}))}{0.23026} \quad (7)$$

198 Setting “B” (Eq. 4 & Eq. 5) to equal “y” decreases the transmission loss according to a specified
199 probability/risk of exceedance. We have set 1 % as this probability of exceedance. “B” will be then
200 be 6.6 dB (set $P_{I>y}$ in Eq. 6 to 0.01). This reduces the transmission loss by 6.6 dB, making the
201 impact area larger, inflating SRI.

202 While adding this probability of exceedance increases the complexity the calculation, we argue that
203 it’s valuable to add a correction that addresses the fact that a simple log(range) transmission loss
204 will under-predict some values in the sound-field, especially for impulsive sources over hard
205 sediment (Figure 4).

206 We acknowledge that this approach severely *under-predicts* transmission losses for softer
207 sediments, but argue that for a simplistic tool that aims to *index* an activity, it is desirable to work
208 from a point of minimal theoretical transmission loss. The additional benefit is that using the tool
209 with this propagation model will give the user an insight into a worst-case impact for the activity.
210

211 Figure 4. Effect of applying correction factor “B”. Modelling for data series “Basalt”, “Moraine” and
 212 “Sand” with dBSeaPE (Parabolic Equation method) to show effect of sediment as well as effect of
 213 changing “B”. Attenuation from absorption is ignored in this example due to the low frequencies
 214 modelled. Green line is example of a semi-spherical transmission loss with attenuation and channel
 215 leak estimated at 1.5 dB/km. The two series named “Model” are the model used in this framework with
 216 and without the correction term “B” applied.



217
 218 For the proponent of the noisy activity this approach can seem to unjustly associate a higher-than-
 219 realistic SRI value with the activity, but the SRI is first and foremost an index, the application to
 220 real-world scenarios is not the focus.

221 4.1 THE SRI TRANSMISSION LOSS MODEL

222 The above introduced model does not directly account for the high attenuation of high frequencies
 223 due to absorption, and further does not predict transmission losses at short ranges well. This is the
 224 basis for the following modifications to the model.

225 4.1.1 Absorption

226 Attenuation from absorption is evaluated for the centre frequency of each octave- or 3rd-octave
 227 band (depending on user choice) according to methods from (Ainslie & McColm, 1998).

228 4.1.2 Short Range Transmission Loss

229 For calculating transmission losses at short range, we introduce a modified transmission loss
 230 model. This is due to excessive transmission loss caused by the term “ $10 \text{Log}_{10} \left(\frac{D}{2} \right)$ ” in Eq. 4, p. 10.
 231 At large depths this term will bring high transmission losses, exceeding a “ $20 \text{Log}_{10}(\text{range})$ ” model.

232 For example, at range 10 m and depth 500 m the transmission loss is predicted as 27 dB. This is
 233 7 dB more than with a spherical model.

234 For ranges shorter than the depth we thus use the range, “ r ”, in place of the depth:

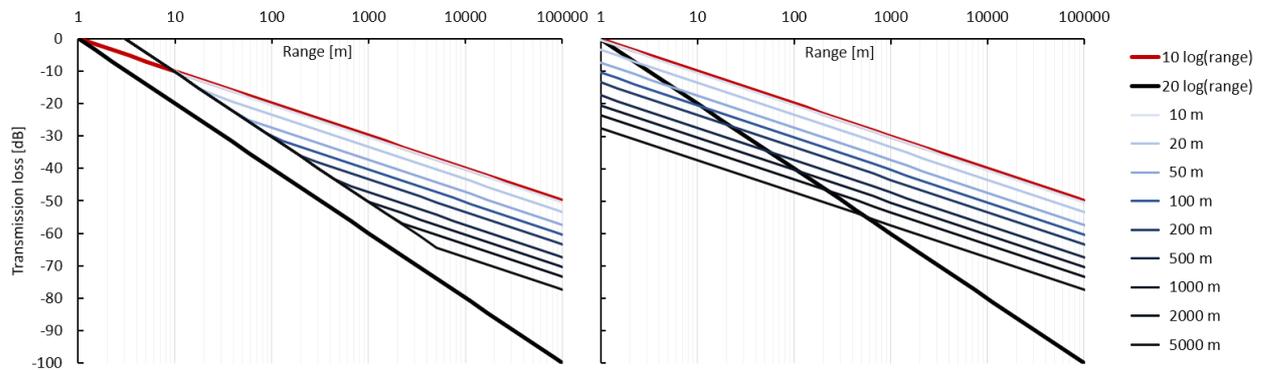
$$\begin{aligned}
 D > r &\rightarrow TL = 10 \cdot \text{Log}_{10}(r) + 10 \cdot \text{Log}_{10} \left(\frac{r}{2} \right) - B + \alpha \\
 D < r &\rightarrow TL = 10 \cdot \text{Log}_{10}(r) + 10 \cdot \text{Log}_{10} \left(\frac{D}{2} \right) - B + \alpha
 \end{aligned}
 \tag{8}$$

235
 236 “ D ”, depth at source position. “ r ”, range. “ TL ”, Transmission Loss. “ B ”, correction term (see chapter
 237 4.0). “ α ”, absorption.

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 239

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Figure 5. Comparison of transmission loss between adjusted (left) and non-adjusted model (right). For large depths the unadjusted model yields transmission losses larger than spherical spreading. The adjusted model predicts transmission losses equivalent to spherical spreading minus 10 dB until depth is larger than range.



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4.2 IMPULSE NOISE PROPAGATION

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When impulsive noises or “transients” propagate, the actual sound pressure at any given range and depth can vary considerably from what is expected from spreading and absorption. As an omnidirectional source (monopole) emits an impulse, that impulse will interfere with itself and give rise to volumes of higher pressure where constructive interference occurs, and correspondingly volumes where destructive interference occurs, resulting in lower pressure. As we are interested in establishing what the highest likely pressure will be, we cannot ignore this effect, and this is in part where the term “B” in the above section comes from (it relates to energy distribution in the water volume). Due to boundary interaction the impulse quickly becomes “stretched” in shallow scenarios and is in the tool simply modelled as any other source.

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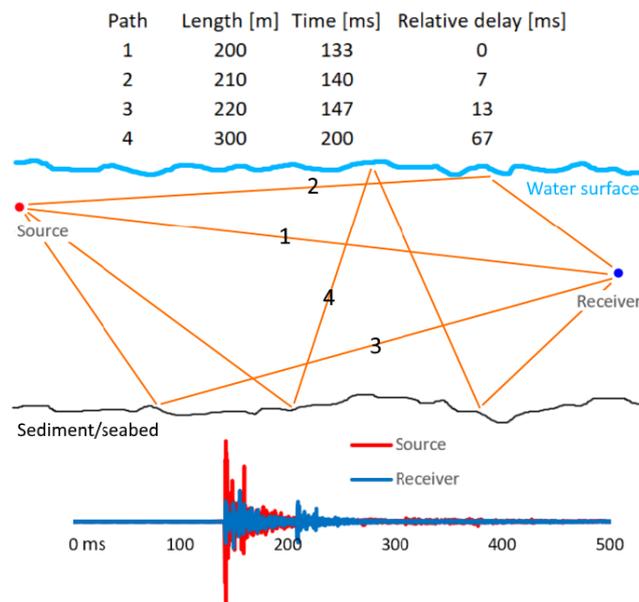
We investigated (APPENDIX I) the rate of “stretching” for an impulse in order to establish when an impulsive noise is better characterised as a continuous noise at long range due to reflections and accumulated interference (Figure 6, p. 12). We found no good model to predict this, and so a crest factor, calculated from the waveform, is applied to impulsive signals and thresholds associated with impulsive noise should be used.

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It should be pointed out that under real life conditions, with many factors increasing signal degradation, we expect that for certain conditions it would be fair to characterise the received signal from a distant impulse as a continuous noise, but this is not done in this framework.

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Figure 6. Boundary reflections lead to the signal being "stretched", so the energy is spread temporally with the impulse losing its initial shape.



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266 **4.3 POST-PROCESSING**

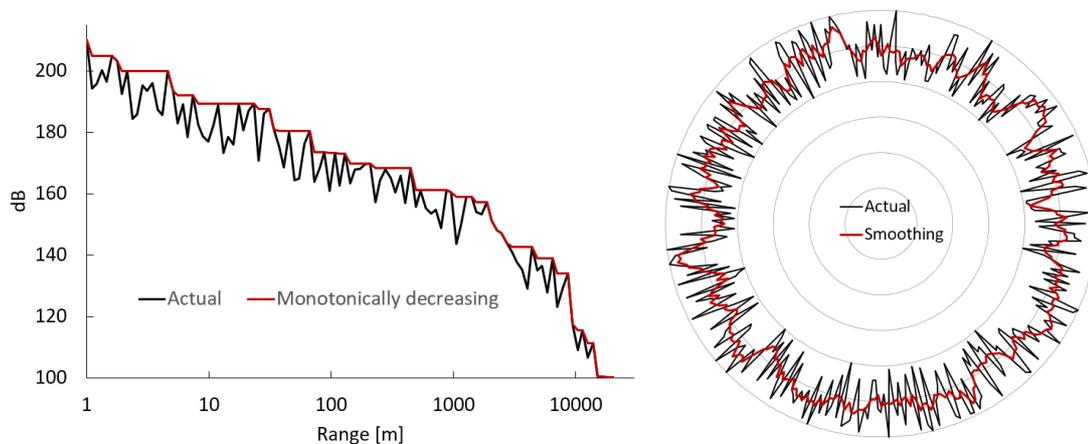
267 To go from a fully calculated sound field to an SRI-level some processing is done to interpret the
 268 results and add some conservative measures.

269 *This will seldom change the results as semi-spherical transmission loss modelling already
 270 decreases monotonically from the source and is radially symmetrical.*

271 **4.3.1 Smoothing of results**

272 Two methods are used to smooth results before using them to calculate the SRI: Making the
 273 results monotonically decrease and smooth the results radially. Both can be tuned by the user if
 274 they wish to do so.

275 **Figure 7. Examples of post-processing with smoothing kernels. Left shows the application of a filter to**
 276 **ensure monotonically decreasing values, while the right chart is an example of a radial smoothing**
 277 **kernel (running mean type).**



278
 279

280 **5.0 USER INPUTS**

281 **5.1 SOUND SOURCE**

282 **5.1.1 Source level and spectrum**

283 The user can input a custom level and/or spectrum in the range 12.5 Hz to 168 kHz in octave- or
 284 3rd octave-bands. The user can also choose from a range of predefined noise sources (e.g. generic
 285 pile driving, seismic array or a vessel) and then adjust the broadband level to match the desired
 286 level.

287 The source level can be entered as either dB_{SEL} , $dB_{RMS-1000}$ or as intensity, dB re 1 μW .

288 **5.1.2 Crest factor of the source**

289 If the source is known to contain peaks that are not captured by the $dB_{RMS-1000}$ level, the user can
 290 add information about the extent of these here. The crest factor is simply the number of dB
 291 between the maximum pressure level and the RMS-level of the sound.

292
$$dB_{crest\ factor} = dB_{z-p} - dB_{RMS} = dB_{p-p} - 6.02^7 - dB_{RMS} \quad (9)$$

293 If the crest factor is given by the user a dB_{z-p} and dB_{p-p} will be calculated from this.
 294 The default value for the crest factor is 0 dB. Note that signal symmetry about ambient pressure is
 295 assumed unless a pressure-timeseries is loaded into the tool.

296 If the user knows that the source is impulsive, the option to import a timeseries into the tool should
 297 be used as this automatically will choose the correct limits and levels for the source type, as well
 298 as calculate dB_{SEL} and crest factor.

⁷ Only valid if signal is symmetrical in pressure fluctuations about ambient pressure.

299 **5.1.3 Impulsive source**

300 For impulsive sources a timeseries (pressure vs time) can be imported (i.e. a single representative
301 impulse from the activity).

302 The tool will use a filter-bank (Butterworth filters, 3rd order) to estimate the per-band dB_{SEL} level as
303 well as dB_{z-p} and dB_{p-p}.

304 Note that for the SRI tool this approach will ignore phase information in the given timeseries when
305 applying the propagation model. The impulse is converted into a series of band levels and this is
306 used for calculation. The crest factor from the timeseries is applied to estimate dB_{z-p} and dB_{p-p}.

307 **5.1.4 Simplified Seismic Source Level Calculator**

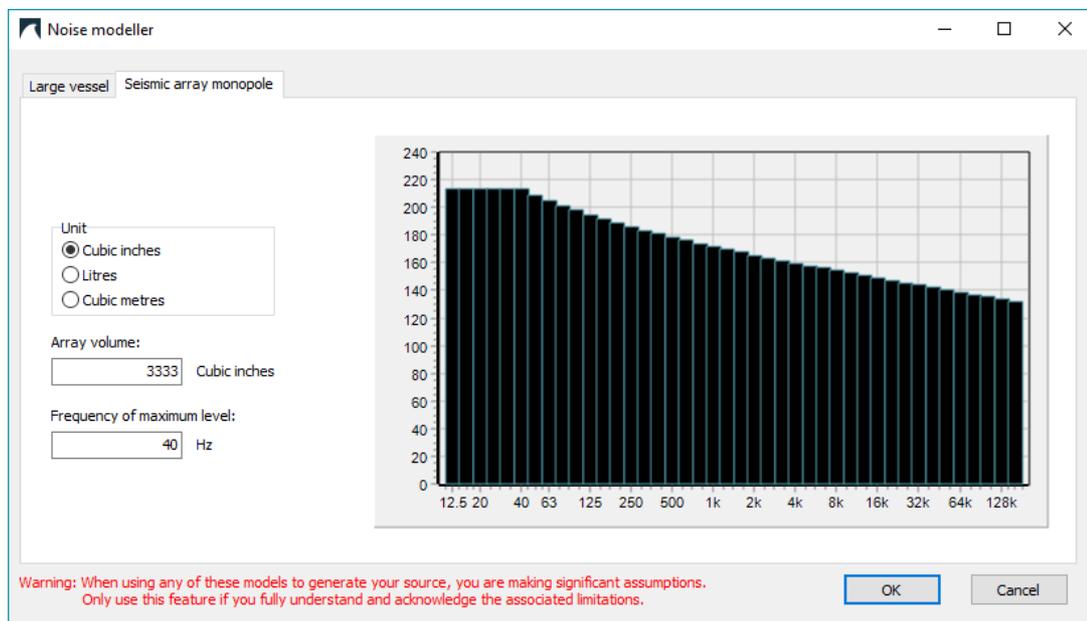
308 For seismic sources where only the volume of the array is known we include an option to enter the
309 array volume and the tool will calculate an equivalent point source based on this. The method is
310 very crude by design and based on generalising data from published seismic array far-field levels
311 (Cotton, 2003; Sutton, Jessopp, Clorennec, & Folegot, 2014). Not much information is available
312 regarding the operation pressure of the arrays used to generate this model. Cotton 2003 states
313 that 2000 psi was used in all 13 arrays in their study, while the Sutton et al. 2014 review uses
314 data from a variety of sources, one of which states the operating pressure to be approximately
315 1900 psi. The remaining data is from field recordings where no information about operating
316 pressure was available to the authors. While operating pressure affects the source level, there
317 seems to be good agreement between array volume and equivalent source level in real scenarios,
318 and so for this very simplified approach only volume is used.

319 Curve fitting lead to Eq. 10 that produces a dB_{z-p} within 1.3 dB of the observed values (from
320 publications mentioned above) in the frequency range 40 Hz to 63 kHz.

$$321 \quad dB(V_{Ci}, f_{Hz}) = -16 \cdot \log_{10}(f_{Hz}) + 150 \cdot f_{Hz}^{-0.5} + 32.5 \cdot \log_{10}(V_{Ci}) + 100.5 \quad (10)$$

322 Volume “V_{ci}” is given in cubic inches and frequency in Hz.
323

324 **Figure 8. Example of a menu from the SRI software.**



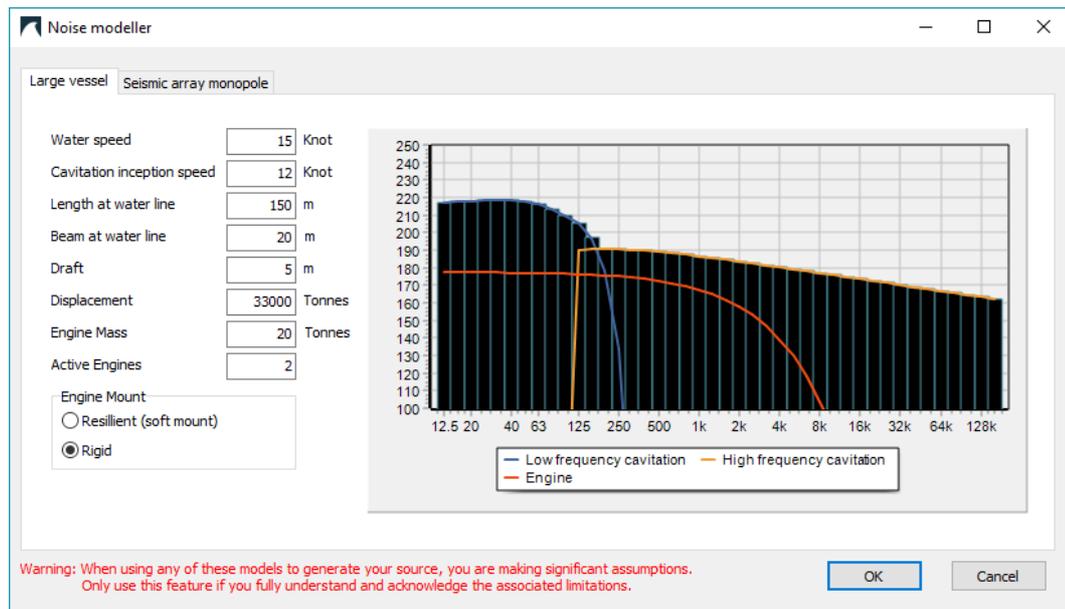
325
326 Please note that we have limited the level at the lowest frequencies. This is done as Eq. 10
327 generally overpredicts levels at very low frequencies (< 40 Hz), frequencies that would otherwise
328 have a large impact on the calculated impact ranges.

329 **5.1.5 Large vessel noise model**

330 Additionally, we have implemented a source generator for large vessels following the model by
331 (Wittekind, 2014) to facilitate use of realistic sound sources, should the user not have their own
332 data. This model takes input about the vessel and engine size along with design information about
333 operating speeds and engine mounting method.

334

Figure 9. Example of a menu letting the user generate a large vessel noise source.



335

336 5.2 ENVIRONMENT AND SCENARIO

337 The user has options to include a limited amount of information about the environment of the
338 proposed activity.

339 5.2.1 Bathymetry

340 The user can specify the bathymetry of the scenario by importing data files containing depth
341 information or generate their own representative scenario.

342 5.2.2 Frequency range and absorption

343 To estimate absorption from magnesium sulphate and boric acid equations from (Ainslie &
344 McColm, 1998) are used. The user can further specify water temperature and pH, but this will only
345 affect results marginally.

346 Frequency range is determined by the user – 12.5 Hz to 168 kHz is available.

347 5.3 RECEIVERS AND LIMIT TYPES

348 Besides the source level and spectrum and transmission loss, the receiver’s limit and frequency
349 specific sensitivity is what determines the SRI value.

350 The tool is set up to either use no acoustic weightings or to apply acoustic weightings to the results
351 prior to using a limit to calculate an area. Weightings should here be understood similarly to e.g. A-
352 weightings for humans, in that they are not directly related to the hearing threshold, but rather
353 mimics the general form. Their application yields a weighted noise spectrum, dB(A) for an A-
354 weighted noise level. In the separate report “Methods for the SRI-tool” we introduce a range of
355 suggested weightings covering marine macro-fauna, and here we will only go through the method
356 of applying multiple weightings and limits rather than justify the choice of any specific weightings.

357 5.3.1 Receiver weightings and limits

358 We will use two species groups, “Low” and “High” to illustrate how we apply weightings and limits.
359 In this framework we have adopted the equations from the work by NMFS and NOAA (NOAA, 2018),
360 as it allows us to have a consistent approach to all hearing groups using the general equation on
361 page 13 of the guidance document (NOAA, 2018). Note that the weightings suggested by Southall
362 et al in 2019 are identical to these, only the naming differs (Southall, et al., 2019).

363

$$E(f) = K - 10 \cdot \log_{10} \left(\frac{\left(\frac{f}{f_1}\right)^{2a}}{\left(1 + \left(\frac{f}{f_1}\right)^2\right)^a \cdot \left(1 + \left(\frac{f}{f_2}\right)^2\right)^b} \right) \quad (11)$$

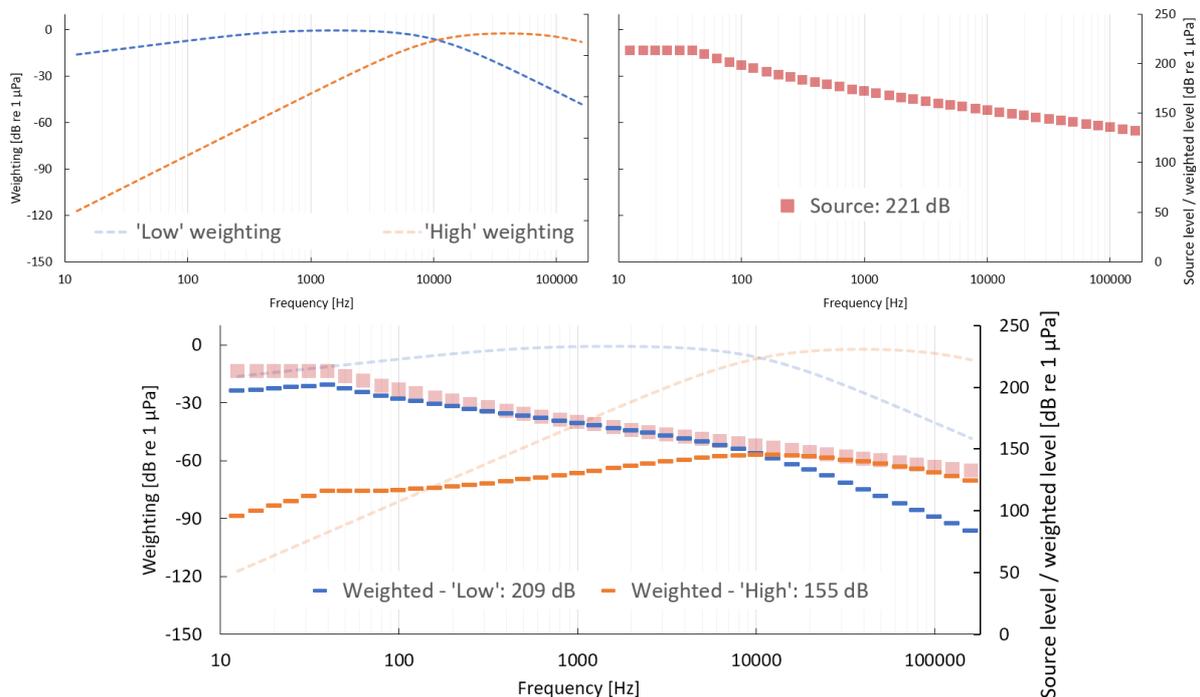
364

365 “E” is a detection limit in $\text{dB}_{\text{RMS-1000}}$ at a specified frequency. “K” is a vertical offset to adjust the
 366 minimum weighting level. “a” determines low-frequency roll-off in sensitivity ($20 \cdot a$ dB/decade).
 367 “b” determines high-frequency roll-off in sensitivity ($20 \cdot b$ dB/decade). Lower and higher “limit” of
 368 best hearing are given by “ f_1 ” and “ f_2 ”.

369 After received levels have been determined across the scenario, weightings for each included
 370 receiver type are applied to find weighted broadband levels throughout the scenario.
 371 Weightings are applied for the centre frequency of either octave- or 3rd-octave bands.

372 Specific group limits are evaluated against the group-weighted broadband level to establish the
 373 range to the limit.

374 **Figure 10. Example of two weightings (Eq. 11) being applied to a 3rd octave band spectrum. Levels**
 375 **given in legend are broadband levels while axes show band levels or weighting levels.**
 376 **Top left: Weightings. Top right: Source. Bottom: weighted level.**



377

378 If we set limits for group “Low” and “High” to be 170 dB and 160 dB respectively, we will see that
 379 even though group “High” has a lower limit of 160 dB, the weighting means that the limit is not
 380 exceeded (Figure 10 above & Table 2 below). The range to the limit of “Low” is ~725 m, leading to
 381 an SRI of 0.73 for the “Low” group. The group “High” here has an SRI of “0”.

382 **Table 2. Overview of "Low" and "High" group limits and weighted levels.**

Group	Limit [dB_{SEL}]	Weighted level [dB_{SEL}]	Limit exceeded?
Low	170	209	Yes (39 dB)
High	160	155	No (-5 dB)

383

384 Please see the “SRI Methods” document for real world examples.

385

386 **6.0 CONCLUDING REMARKS**

387 The example above concludes this report, describing the theory of the framework used to
388 compress and integrate noisy activity information into a single Sound Risk Indicator. It is not
389 intended as a replacement for impact assessments, but rather to serve as an indexing tool to let
390 industry and regulators easily compare various scenarios by assigning a single number to them.

391 We invite readers of this document to send comments and questions to:

392

393

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Rasmus Sloth Pedersen

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482 Appendix I – Sound impulsivity.

483

484 When an impulse propagates through an environment it undergoes self-interference. This process works to
 485 “stretch” the impulse, meaning that a receiver will be exposed to a lengthened and “smeared out” version
 486 of the initial impulse. We here present the background for investigating whether this effect can be
 487 generalised to calculate a range at which the impulse is so stretched that it is better characterised as a
 488 continuous noise. All calculations assume that the sound speed is constant, depth is constant, that there is
 489 no absorption and there is perfect reflection at boundaries (air-water interface inverts signal).

490 1 ESTIMATION OF PROPORTION OF WAVEFRONT THAT HAS BEEN 491 REFLECTED

492 In a scenario with perfectly reflecting sea surface and sediment we can calculate the proportion of
 493 a wave-front that arrives at a range without having been reflected (Figure 1.1 & Eq. 1 & 2). This is
 494 interesting as the initial wavefront will experience at least spherical spreading loss (Eq. 1), a rate of
 495 attenuation much greater than the “spherical-cylindrical” approach often used (Eq. 2).

$$496 \quad TL_{sph} = 20 \cdot \log_{10}(range) \quad (1)$$

$$497 \quad TL_{s+c} = 10 \cdot \log_{10}(range) + 10 \cdot \log_{10}(k) \quad (2)$$

498 “ TL_{sph} ”, spherical transmission loss; “ TL_{s+c} ”, spherical-cylindrical transmission loss; “ k ”, transition
 499 range where transmission loss goes from spherical to cylindrical.

500 Proportion of wavefront reflected at least once, assuming flat bathymetry:

$$R_1 = 1 - (fraction\ not\ reflected\ from\ surface) - (fraction\ not\ reflected\ from\ bottom)$$

$$501 \quad R_1 = 1 - \frac{\sin^{-1}\left(\frac{S_D}{R_h}\right) - \sin^{-1}\left(\frac{D - S_D}{R_h}\right)}{\pi} \quad (3)$$

502 For spreadsheet:

$$503 \quad "=1-IF(R_h>S_D,ASIN(S_D/R_h)/PI(),0.5)-IF(R_h>(D-S_D),ASIN((D-S_D)/R_h)/PI(),0.5)"$$

504 The “ASIN” function does not tolerate inputs ≥ 1 so IF-statements are necessary.

505 “ R_1 ” being proportion of wave-front that has been reflected at least once, “ S_D ” is source depth, “ R_h ”
 506 is horizontal range from source, “ D ” is depth at source.

507 Equation (1) above can be expanded to accommodate more reflections:

$$511 \quad R_{n_{rfl}} = 1 - \frac{\sin^{-1}\left(\frac{S_D + D(n_{rfl} - 1)}{R_h}\right) - \sin^{-1}\left(\frac{D - S_D + D(n_{rfl} - 1)}{R_h}\right)}{\pi} \quad (4)$$

508 For spreadsheet:

$$509 \quad "=1-IF(R_h>S_D+D*(n_{rfl}-1),ASIN((S_D+D*(n_{rfl}-1))/R_h)/PI(),0.5)-IF(R_h>(D-S_D+D*(n_{rfl}-1)),ASIN((D-
 510 S_D+D*(n_{rfl}-1))/R_h)/PI(),0.5)"$$

512 “ $R_{n_{rfl}}$ ” (n -reflections) is the proportion of the wavefront that has been reflected “ n_{rfl} ” times. From
 513 the above we can establish that, at a range equal to 5 times the depth:

514 94 % of the wave-front has been reflected at least once (meaning 6 % has not been reflected at
 515 all).

516 80-81 % has been reflected at least twice.

517 66-67 % has been reflected at least thrice.

518 50-51 % has been reflected at least four times.

519 20-29 % has been reflected at least five times.

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Table 3. Example of application of Eq. 2 to calculate the proportion of a wave-front that has experienced a given number of reflections at a given distance. The distance is given as Range/Depth as the results are dependent on that ratio rather than their absolute values.

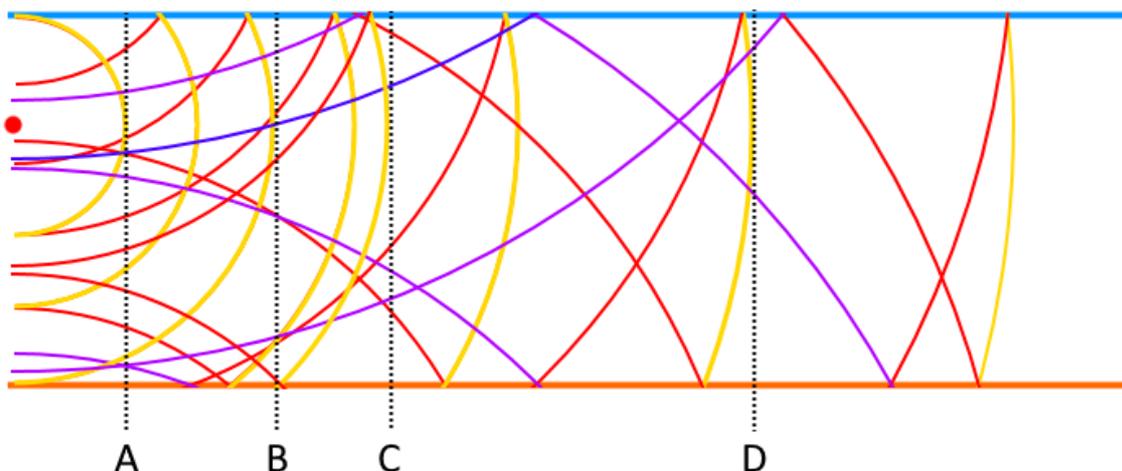
		Range/Depth							
		0.10	0.50	1.00	2.00	2.50	3.15	4.0	5.0
Number of reflections experienced by wave-front	0	91%	67%	38%	16%	13%	10%	8%	6%
	1	9%	33%	62%	41%	29%	22%	17%	13%
	2	0%	0%	0%	42%	45%	28%	19%	14%
	3	0%	0%	0%	0%	14%	37%	27%	16%
	4	0%	0%	0%	0%	0%	3%	29%	24%
	5	0%	0%	0%	0%	0%	0%	0%	26%
Sum		100%	100%	100%	100%	100%	100%	100%	100%

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Figure 11. Schematic of a wave-front moving away from a source, when bounded by two perfectly reflecting surfaces (8 time-snapshots). Yellow arcs are direct part of original impulse, red arcs have been reflected once, purple arcs twice and blue arcs thrice. Point "A", at range equal to source depth, no part of the impulse arriving here at this time has been reflected and the impulse retains its original "form". Point "B", at range equal to source depth minus total depth, this is the maximal possible range for not having any part of the wave-front being reflected (in the case of source depth = total depth/2). Point "C", range equal to depth, 50-67 % of the wave-front has now been reflected at least once. Point "D", range equal to 2 x total depth, 83-84 % of the initial wave-front has now been reflected at least once. At point "D", a maximum of 17 % of the wave-front has arrived directly, with no reflections.

- Direct (no reflections)
- 1 reflection
- 2 reflections
- 3 reflections



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On the basis of the above, we speculated that as only the initial wavefront retains its original shape, but with a high transmission loss of $> 20 \times \log_{10}(\text{range})$, a receiver at a range of $5 \times \text{depth}$ would experience the impulse as a series of smaller impulses with peak pressures as predicted by spherical spreading, but exposure as predicted by Eq. 2. We hoped to use this approach to investigate how the crest factor ($\text{dB}_{z-p} - \text{dB}_{\text{RMS}}$, as a proxy for impulsiveness) developed with increasing number of reflections and range.

541

The definition of impulsiveness in the literature is precariously ambiguous:

542 ISO 1996-1:2016 (3.5) states that:
 543 “At the time of publication of this part of ISO 1996, no mathematical descriptor exists which can
 544 define unequivocally the presence of impulsive sound or can separate impulsive sounds into the
 545 categories given in 3.5.1 to 3.5.3.”

546 The British standard “BS 4142:2014” defines impulsiveness by the use of dB_{RMS} with a 50 ms
 547 window and the change in tangent slope versus time (10 dB/second). This is however unsuitable
 548 for our application, as a 50 ms integration window is too slow to represent the very short
 549 integration times found especially in marine mammals. This line of investigation was abandoned
 550 as the 10 dB/second limit proved unrealistic for integration times shorter than 50 ms.

551 We then looked to get to a crest factor less than 6 dB, but this was also unrealistic, and so this
 552 approach abandoned.

553 This leads to the next section where we calculate the travel times for a seismic source impulse and
 554 sample the resulting sound field.

555 2 ESTIMATING TIME DELAY FROM RAY PATHS

556 By calculating the length of various transmission paths, we can calculate the relative arrival time of
 557 an emitted impulse and thereby investigate the received time-pressure signal considering
 558 interference. We assume no refraction in the following.

559 For a sound to be reflected e.g. three times it has bounced of the boundaries (surface & sediment)
 560 three times (the order depending on whether it hit the surface or the sediment first. (Figure 16 C).

561 Those bounces lead to a minimal additional distance to travel when compared to a path that
 562 hasn’t bounced.

563 First, let’s calculate the length of the direct path:

$$564 \text{ Direct Path} = \sqrt{(S_D - R_D)^2 + R_h^2} \quad (5)$$

565 “S_D” source depth, “R_D” receiver depth and “R_h” horizontal range. Any path other than the direct
 566 will have travelled longer due to its path travelling to either boundary (surface or sediment) at least
 567 once. The length of that path can be similarly calculated:

$$568 \text{ Odd Bounce Path} = \sqrt{(S_D + R_D + n_B \cdot D - D)^2 + R_h^2} \quad (6.1)$$

$$569 \text{ Even Bounce Path} = \sqrt{(S_D - R_D + n_B \cdot D)^2 + R_h^2} \quad (6.2)$$

570 “D” being depth, “R_h” is horizontal range and “n_B” is number of bounces.

571 Note that “S_D” and “R_D” are source distance to boundary of first reflection and can be either
 572 surface or bottom.

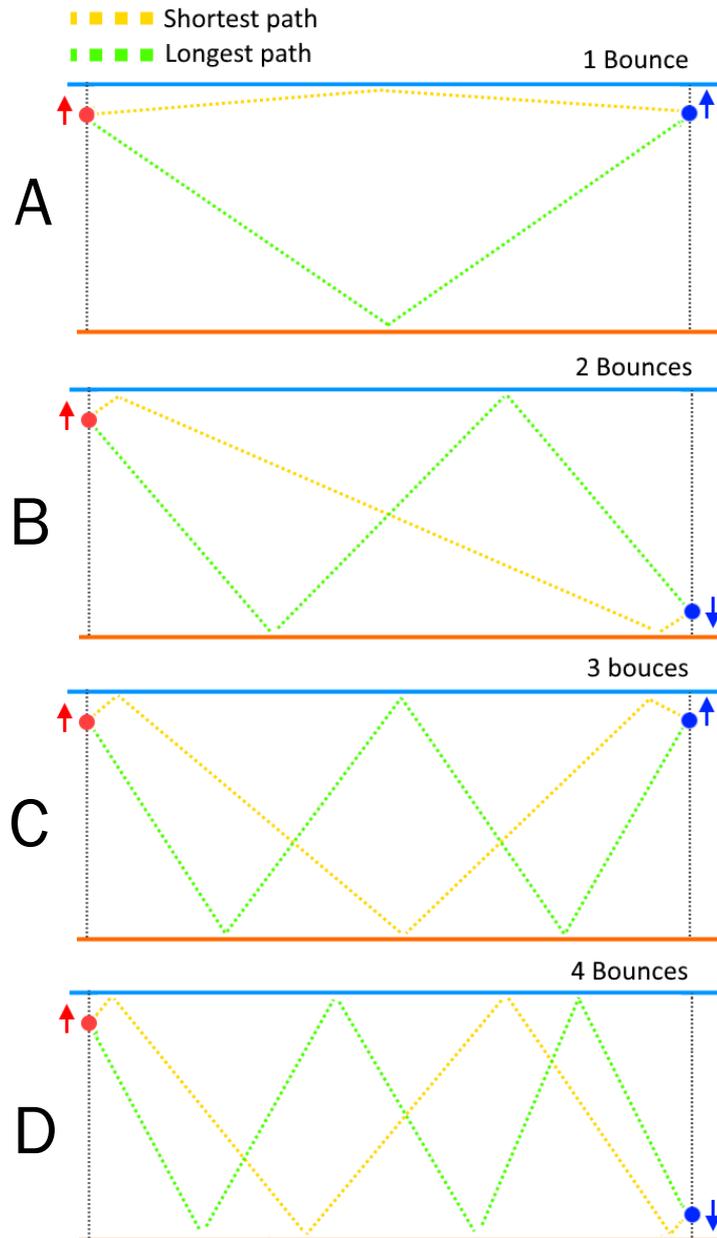
573 The shortest path with three bounces (or any odd number) exists when S_D and R_D approach the
 574 same boundary (either surface or bottom) and their distance to that boundary decreases towards
 575 zero (Figure 16 C), meaning that the shortest path with n_B bounces at limit is:

$$576 \text{ Bounces Shortest Path} = \sqrt{((n_B - 1) \cdot D)^2 + R_h^2} \quad (7)$$

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Figure 12. Ray paths for two to four bounces. Notice that as the source (red) and the receiver (blue) move in direction of the arrows, their shortest path length becomes equal to that of the longest path with 2 fewer bounces.



581

582 For an even number of bounces the situation is slightly different in that the shortest path for an even
583 number of bounces exists when the source and the receiver are at opposite boundaries (Figure 16 B & D).
584 This however, results in the same relationship as for odd bounces (Eq. 7). See Figure 16 to graphically
585 confirm this, keeping Pythagoras' theorem ($a^2+b^2=c^2$) for right-angle triangles in mind.
586 For the direct path, with the same source and receiver depths, equation (5) reduces to R_h
587 (as the term $(S_D - R_D)^2$ becomes zero when $S_D = R_D$):

588
$$\text{Direct Path} = \sqrt{R_h^2} = R_h \tag{8}$$

589 With the shortest direct path equal to R_h and the corresponding shortest bounce path from Eq. 7 we can
590 estimate the factor with which the direct path relates to the reflected path.

591
$$F_{n_B} = \frac{\sqrt{(n_B - 1) + \left(\frac{R_h}{D}\right)^2}}{\left(\frac{R_h}{D}\right)} = \frac{R_{reflected}}{R_{direct}} \tag{9}$$

592 In the worst-case scenario⁸ R_{direct} is equal to R_h (Figure 16 A) and we can calculate the additional travel and
 593 thereby the impulse delay “ I_d ” in milliseconds by modifying Eq. 9 slightly:

594
$$I_d(R_h, D, n_B) = R_h \cdot \left(\frac{\sqrt{(n_B - 1) + \left(\frac{R_h}{D}\right)^2}}{\left(\frac{R_h}{D}\right)} - 1 \right) \cdot \frac{1500 \text{ m/s}}{1000 \text{ ms/s}} \quad (9.1)$$

595

596 We are now almost in a position to generalise delay times for impulses at any range and depth.

597 For example, at a horizontal range of 1000 meters:

598 **Table 4. Application of Eq. 9.1 to calculate shortest possible delay between first arrival and arrival of**
 599 **subsequent rays. “Dist” is distance travelled for that particular path. The horizontal range is 1000**
 600 **meter throughout.**

Extra distance & delay from reflections		Reflections									
R_h [m]	1000	1		2		3		4		5	
		Dist [m]	Time [ms]	Dist [m]	Time [ms]	Dist [m]	Time [ms]	Dist [m]	Time [ms]	Dist [m]	Time [ms]
Depth [m]	10000	0	0	9050	6033	13177	8785	16349	10900	19025	12683
	2000	0	0	1236	842	2000	1333	2606	1737	3123	2082
	1000	0	0	414	576	732	488	1000	667	1236	824
	500	0	0	118	79	225	150	323	215	414	276
	333	0	0	54	36	106	70	155	103	202	135
	250	0	0	31	21	61	40	90	60	118	79
	200	0	0	20	13	39	26	58	39	77	51
	100	0	0	5	3	10	7	15	10	20	13
10	0	0	0	0	0	0	0	0	0	0	0

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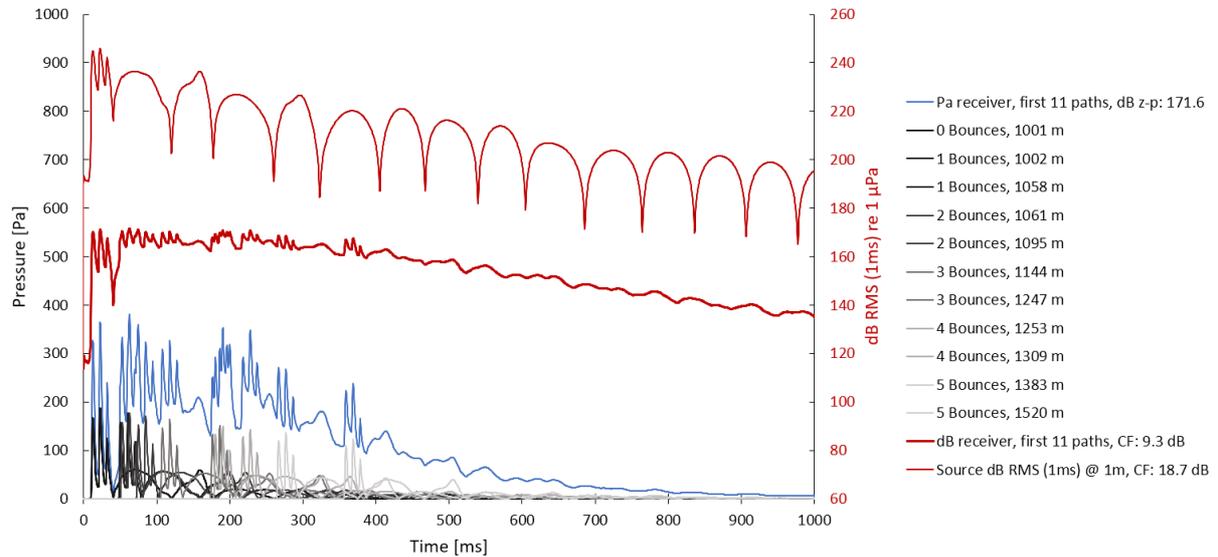
602 We can visualise this by splitting the impulse into rays, apply a delay and transmission loss, and then add
 603 them up at a receiver location, see Figure 17 below.

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⁸ Small difference in arrival time is worst case for summation of energy over a short time duration.

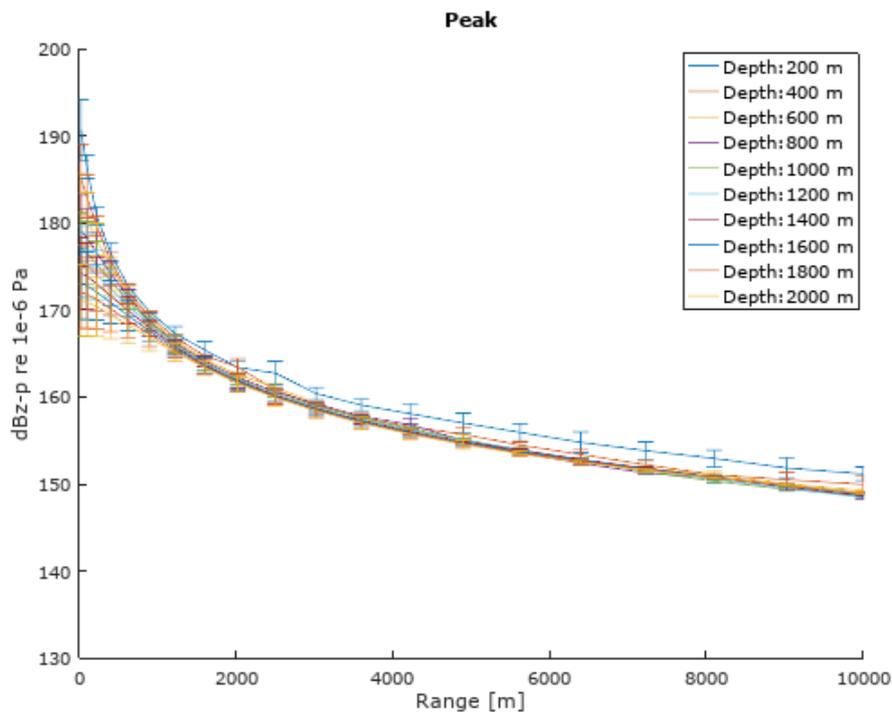
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Figure 13. Example of tracking the first 11 paths from source to receiver (as straight lines, with perfect reflection at boundaries). Range 1000 m, depth 200 m, source depth 5 m, receiver depth 50 m. The source is a 4000 Cui seismic array (thin red line). Notice that the crest factor (CF $dB_{z-p} - dB_{RMS}$) is 18.7 dB at the source, but 9.3 dB at the receiver (thick red line). Red lines read on right axis (dB), remaining lines on left axis (Pa).



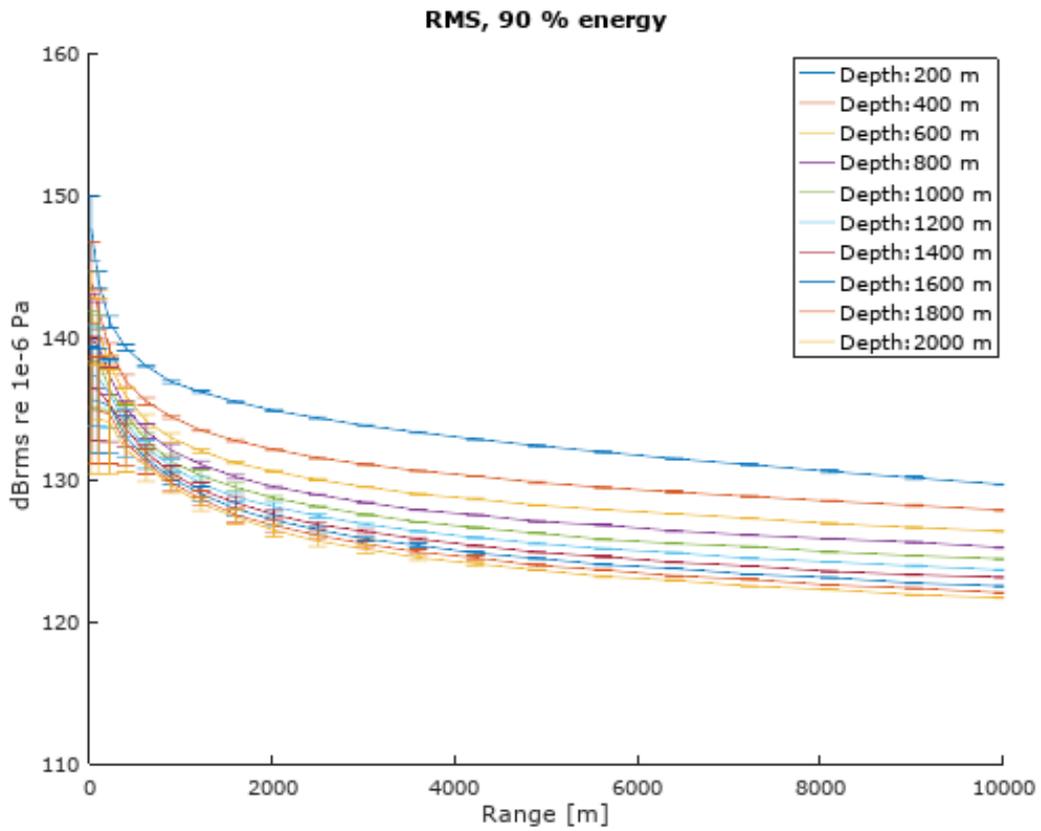
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Taking this a little further, below are the first 41 paths (0-20 reflections). We see that even though the energy gets spread out over a longer duration the signal retains a high crest factor, and so by our own standards remains impulsive. The following 5 charts show various metrics relating to the received signal in 1800 different cases: 20 different ranges, 10 scenario depths and 9 receiver positions (depths) at those ranges. The mean of the 9 receiver depths and 95 % confidence interval is plotted versus the associated horizontal range. Range “0” is zero meters horizontally, not slant range (this explains the large variation at 0 m). Notice that even though “Peak” decreases quicker than “RMS” and “SEL” and the duration of 90 % of the energy is > 1 second for most depths and ranges the crest factor remains high (> 20 dB). We therefore cannot justify treating the signal as a continuous signal and must continue to use appropriate impulsive thresholds when assessing impulses.

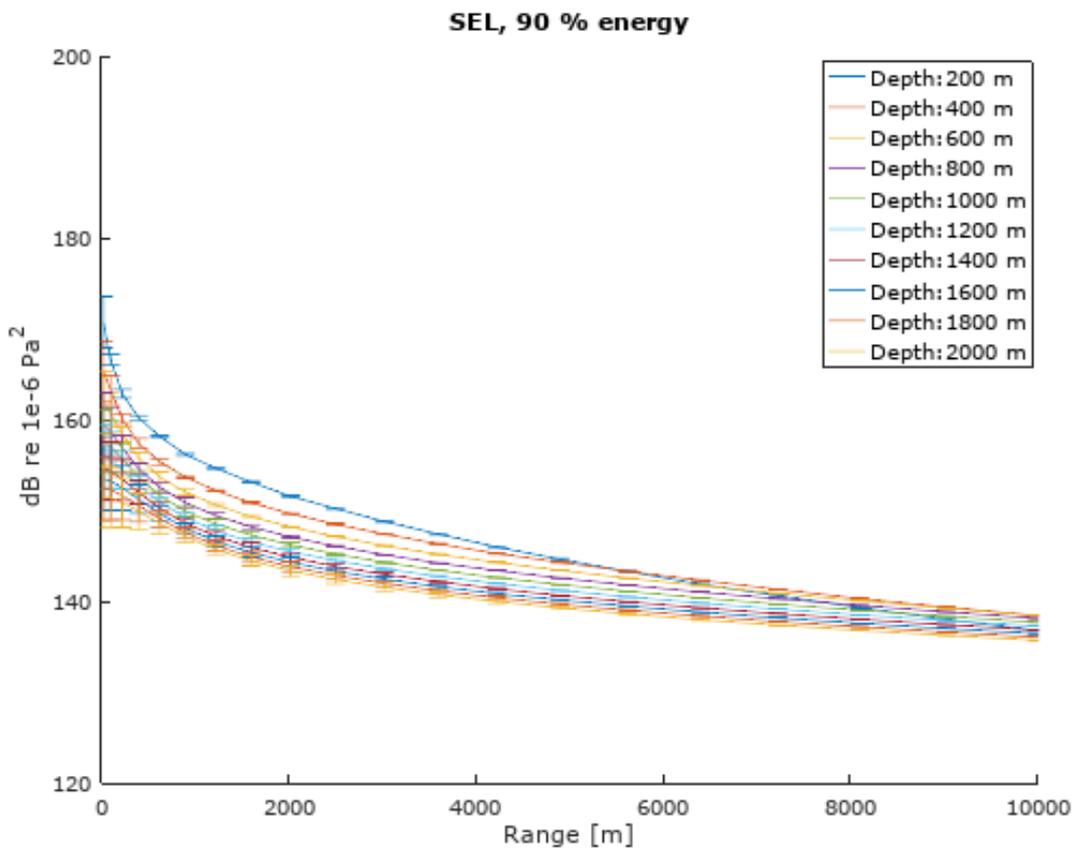


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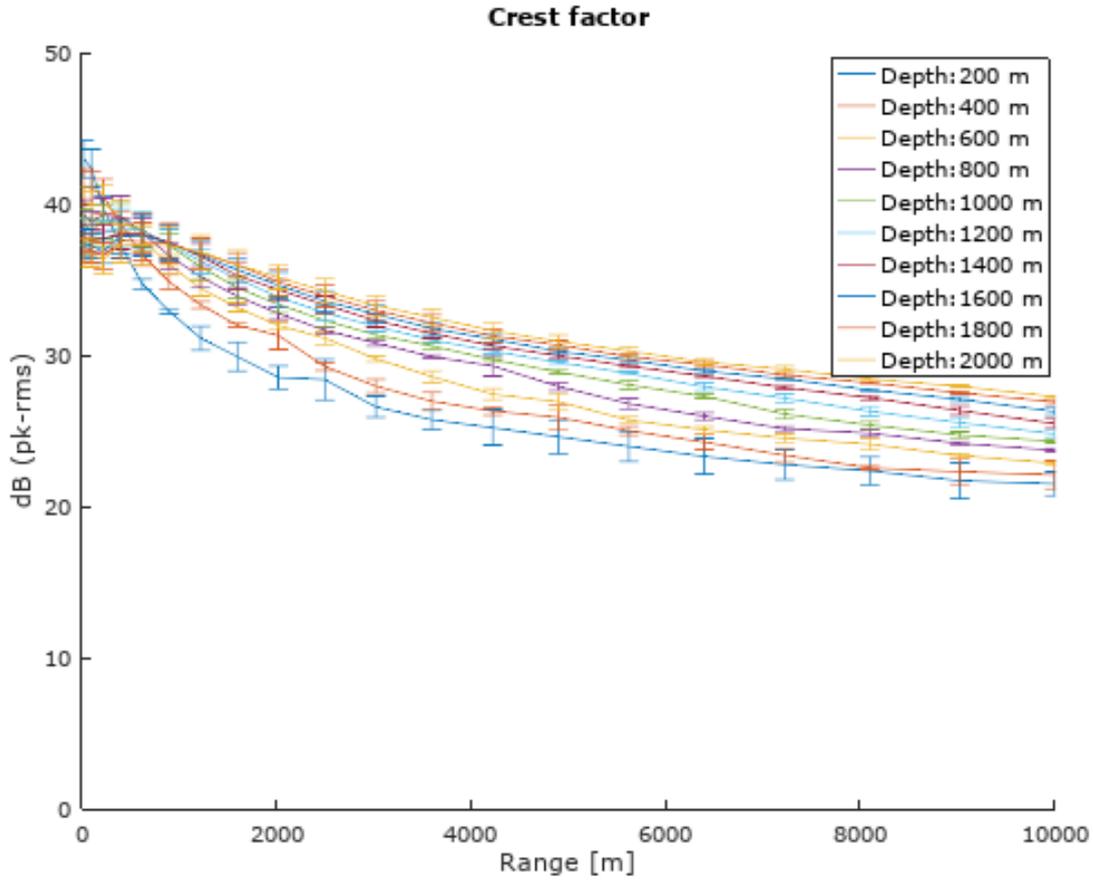
622
623



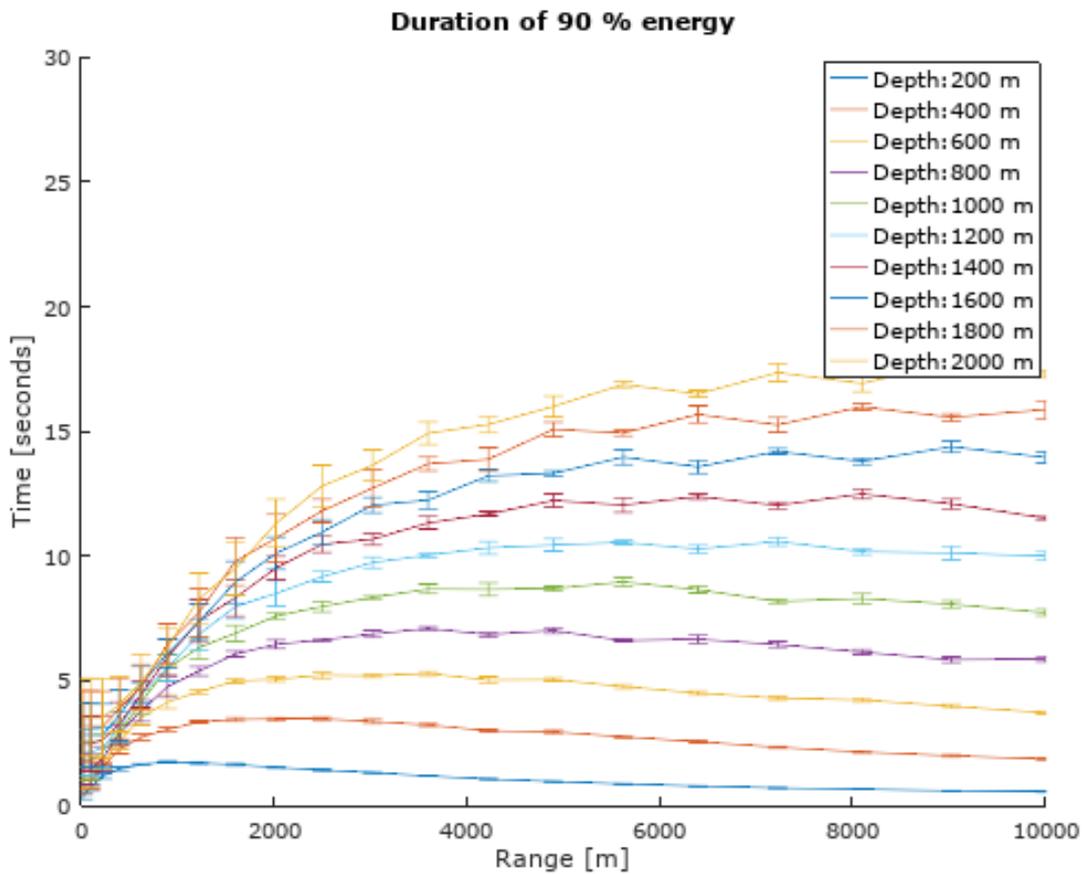
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